TLA2B: A new validation tool for TLA$^+$

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Overview

Approach & Motivation

Approach

Translating the non-temporal part of TLA$^+$ to B

$\Rightarrow$ B does not support temporal formulas

Motivation

- Validating TLA$^+$ specification with existing B tools
- in particular: using the model checker ProB

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TLA$^+$ & B-Method

	TLA$^+$	B-Method
Invented by	Leslie Lamport	J.R. Abrial
State-based	√	√
Set theory	√	√
Predicate logic	√	√
Arithmetic	√	√
Temporal formulas	√	X
State transition	Before-after predicate	Generalised substitutions
Model checker	TLC	ProB
Prove support	TLAPS	AtelierB

MyHourClock

MODULE *MyHourClock*

EXTENDS *Naturals*

CONSTANTS *start*

VARIABLES *hr*

ASSUME $start \in 1 \,..\, 12$

$Inv \triangleq hr \in 1 \,..\, 12$

$Init \triangleq hr = start$

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Concepts of typing

- TLA$^+$ is untyped, while B is strongly typed
- Type informations are needed for the translation
  - B requires type declarations of symbols
  - the translation of some operators depends on them

Type inference algorithm (Hindley-Milner)

- Types of symbols can be inferred by considering the context the symbols are used
  - e.g. x must have the type Integer in the expression $x + 1$
- some resulting restriction for the translation
  - variables must have a fixed type
  - only values of the same type are comparable

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Supported TLA$^+$ values

- The following kinds of values exist in both languages:
  - integers, boolean values, strings, sets, functions, sequences, records
- Restrictions caused by the B type system
  - all elements of a set must have the same type
  - functions and sequences are based on sets
- Model values are translated using enumerated sets

  $\Rightarrow$ the translation conserves symmetry properties

Supported TLA$^+$ operators

- Most TLA$^+$ operators can be mapped to B built-in operators
  - operators of the standard modules Naturals, Integers, Sequences, FiniteSets
- Other operators can be expressed by a combination of B operators
  - e.g. if-then-else
- User-defined operators are translated using B Definitions which are a kind of macro

CHOOSE operator

Its general functionality can not be expressed in B

Standard Module TLA2B

- contains useful operators such as minimum, maximum, sum and product of a set
- this operators can be mapped to B build-in operators

Extending B

- ProB is able to load externally defined (polymorhic) functions
- semantics of the CHOOSE operator is expressed in this way

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Translator: TLA2B

- Automatic translation
- The frontend is based on the parser SANY
- Reuse of TLC's configuration file parser
  - constant/operator assignment and replacement
- Stand-alone translator

Integration of TLA2B into ProB

Applying ProB to TLA$^+$ specification

ProB

- Model Checking
- Constraint-based checking
- Test generation
- Animation
- Visualization

SimpleAllocator case study (by Merz)

- System to manage a set of resources (Rs) that are shared among a number of client processes (Cs)
- The specification allows TLC and ProB to use symmetry

Cs	Rs	TLC		TLA2B + ProB	
		no symmetry	symmetry	no symmetry	symmetry
3	2	<1 s	<1 s	2 s	<1 s
4	3	28 s	2 s	678 s	8 s
5	3	450 s	29 s	-	28 s
6	3	>4200 s	573 s	-	90 s

- Without symmetry TLC is superior to ProB
- For larger set sizes ProB's symmetry outperforms TLC

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Constraint solving

N-Queens:

- Searching for all valid placements of N queens on an N×N chessboard so that no two queens attack each other
- The solution is encoded in a declarative way

N	Solutions	TLC	TLA2B + ProB
6	4	1 s	<1 s
7	40	16 s	<1 s
8	92	375 s	<1 s
9	352	2970 s	<1 s
11	2,680	-	<1 s
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- ProB is supierior to TLC
- searching for a single solution:
  ProB finds a solution for N = 50 in less than a second

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TLA2B + ProB

Demo

- ProB: http://www.stups.uni-duesseldorf.de/ProB/
- TLA2B: http://nightly.cobra.cs.uni-duesseldorf.de/tla/
- Logic Calculator: http://cobra.cs.uni-duesseldorf.de/evalB/

Conclusion & Future work

- Translator TLA2B
  - type inference algorithm
  - supports a large subset of TLA$^+$
- Integration of TLA2B into ProB
  - gain a new tool for TLA$^+$
  - complementary to TLC
- all B tools can be apply to the translated B machine

Future work:

- Testing the correctness of the translation
  - comparing the state spaces generated by TLC and ProB
- Improving and extending the translation
  - support for recursive function

Questions?

if-then-else

- If-then-else is an expression in TLA$^+$

  e.g. IF $x = 0$ THEN 1 ELSE $1/x$

- Cannot use B's if-then-else substitution for translation

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Records

- In B the Type of a record depends on
  - the fields of the record
  - the order of the fields
  - the types of the fields
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  $rec(a : 1) = rec(b : TRUE)$

  $rec(a : \quad , b : \quad) = rec(a : \quad , b : \quad)$
- get a field x of a record r (TLA$^+$: $r.x$)

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  $r'x(TRUE)$

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